

EF03 EW Physics: Heavy flavor and top quark physics

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EF Restart workshop, September 3, 2021

Top and Heavy Flavor Physics

- Prospects for precision measurements (HL-LHC, FCC, ILC, muon collider,...):
 - top quark properties: mass, couplings
 - study of rare processes: single top, ttZ, ttW, tZq, tttt, FCNC, ...
 - precision measurements of a wide variety of observables and in new kinematic regimes: spin correlations, polarization, boosted top, ...
- Joined studies:
 - M_{top} in Global Electroweak fits (with EF04)
 - Top quark couplings and global EFT fits (with EF04)
 - Top and HF in PDF fits: extraction of gluon PDF, alphas, ... (with EF06)
- Prospects for HF physics (b,c,s) at future colliders
 - Full pattern of quark couplings
- Status of predictions and prospects for theory improvements:
 - Interpretation of m_{top} , new ideas for m_{top} measurements
 - Higher order QCD and EW corrections

Opportunities for additional contributions in all areas!

Talk in parallel sessions

Highlights of EF03 activities: m_{top}

- Optimizing top-quark threshold scan using genetic algorithm: Aleksander Filip Zarnecki, Kacper Nowak **Lol**, paper: <https://arxiv.org/abs/2103.00522>
- Limits on Precision Top Mass Measurements at HL-LHC: Stephen Wimpenny
- Measurement of the top quark mass at the ILC: Esteban Fullana , Juan Foster, Frank Simon, Marcel Vos **Lol**
- Top quark mass measurements and their interpretations: Andre Hoang
- Energy Peak and Its Implications on Collider Phenomenology: Top Quark Mass Determination and Beyond: Kaustubh Agashe, Roberto Franceschini, and Doojin Kim **Lol**

Presented at this workshop:

- **Top and HF studies at linear colliders:** Roman Poeschl
- **New ideas for top quark mass measurements:** Kaustubh Agashe

Lol: Letter of Interest

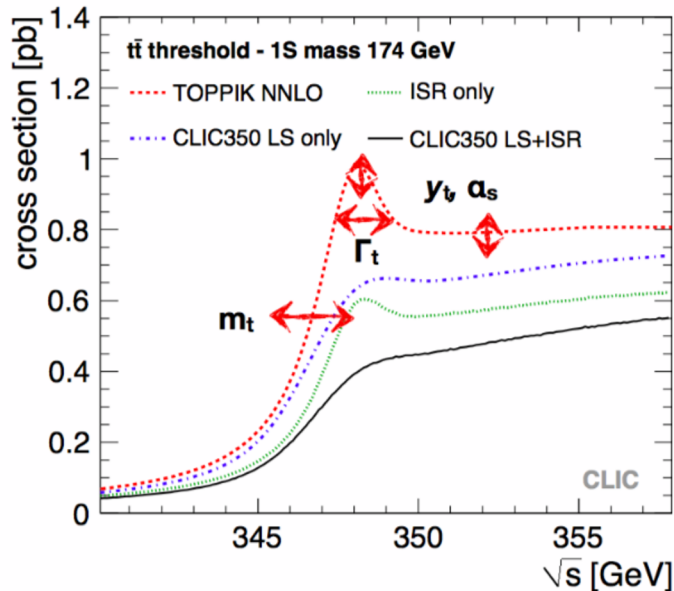
Highlights of EF03 activities: m_{top}

- Top and HF studies at linear colliders: Roman Poeschl

Optimisation of threshold scan using “Non dominated sorting **genetic algorithm**”

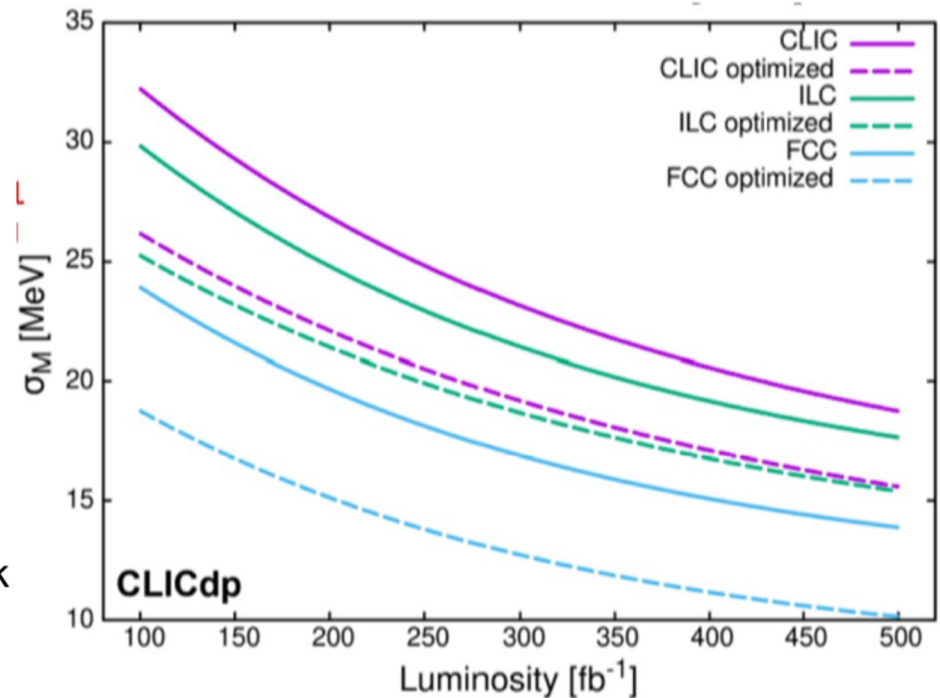
arxiv: 2103.00522

Kacper Nowak, Aleksander Filip Zarnecki



- Effects of some parameters are correlated:
- Dependence on Yukawa coupling rather weak
- Precise external α_s helps

Precision on top mass ...



Highlights of EF03 activities: m_{top}

- New ideas for top quark mass measurements: Kaustubh Agashe

b-jet energy peak method:

implementation on run 1 data in CMS PAS TOP-15-002:

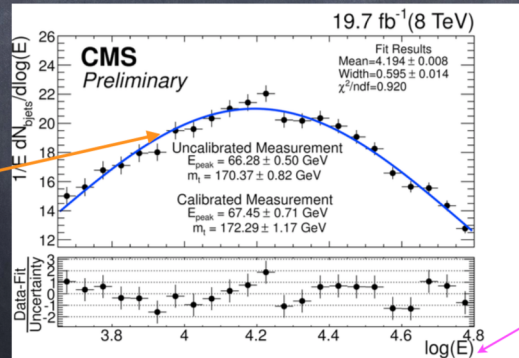
$$m_t = 172.29 \pm 1.17 \text{ (stat.)} \pm 2.66 \text{ (syst.) GeV}$$

Complementary (next slide) to other methods (error ~ 1 GeV)

Sources of error: JES uncertainty; modeling of top p_T

use B -hadron
decay length
(next)

fitting function
(see later)

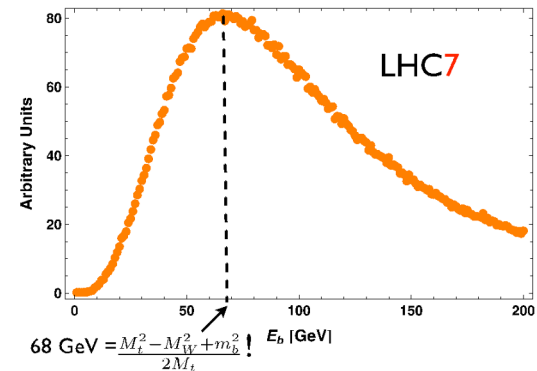


higher-order
(theory)
calculation (KA,
Franceschini, Kim,
Schulze:
1603.03445; see
also Ravasio, Jezo,
Nason, Oleari:
1801.03944 and
1906.09166)

note!

$$E_b^{\text{rest}} = \frac{M_t^2 - M_W^2 + m_b^2}{2M_t}$$

modified vs.
massless



how to “extend” it to B -hadron decay length (correlated with bottom quark energy): circumvent JES uncertainty, “replaced” by hadronization model/fragmentation function (theory improvement possible?)

B-decay length method:

$$G^{\text{fit, us}}(L_B; E_b^{\text{rest}}, w) \approx \int dE_B \int dE_b \frac{1}{N(w)} \exp \left[-w \left(\frac{E_b}{E_b^{\text{rest}}} + \frac{E_b^{\text{rest}}}{E_b} \right) \right] \times D \left(\frac{E_B}{E_b}; E_b \right) \frac{m_B}{c\tau_B^{\text{rest}} E_B} \exp \left(-\frac{L_B m_B}{c\tau_B^{\text{rest}} E_B} \right)$$

(similar procedure to b -jet energy-peak method: different observable and (double) convolution in fitting function)

$G^{\text{fit}}(L_B; E_b^{\text{rest}}, w) \rightarrow$ fitting function for observed decay length (L_B) distribution

Highlights of EF03 activities: Quark polarizations and spin correlations

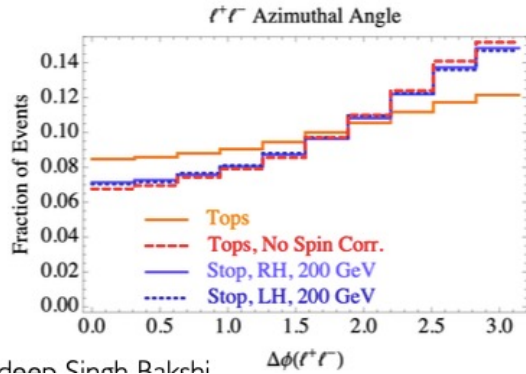
- Quark polarization measurements: from the Standard Model to characterizing New Physics: Mario Galanti, Andrea Giammanco, Yuval Grossman, Yevgeny Kats, Emmanuel Stamou, Jure Zupan **LoI**
- Top Quark and BSM Interactions at the HL-LHC and HE-LHC: Andreas Jung, Alexander Moreno Briceno **LoI**

Presented at this workshop:

- **Top quark spin correlations at the LHC:** Amandeep Singh Bakshi

Highlights of EF03 activities: Quark polarizations and spin correlations

- **Top quark spin correlations at the LHC:** Amandeep Singh Bakshi
 - Very sensitive to BSM physics (s-channel dark matter : more spin correlation, new scalars : less spin correlation)

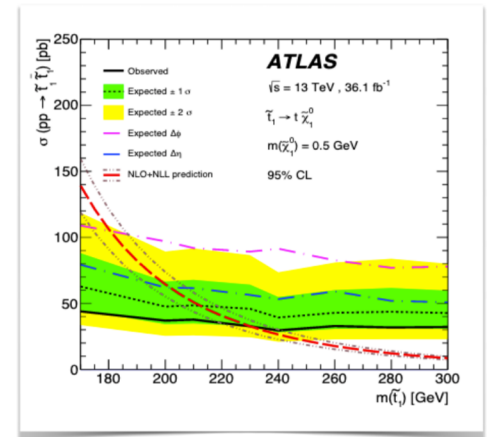


10.1007/JHEP08(2012)083



Plans for Snowmass study

- Set limits in the SUSY top corridor using the spin correlation based DNN.
- Extend phase space beyond stealth corridor region and also study other partners to the top.
- Consider different uncertainty scenarios (full Run2, upcoming Run3 and the HL-LHC) and the impact of major systematics on the limits.
- Our HL-LHC analysis has been pre-approved.
- Could expand into spin density matrix measurement at other colliders/machines: 100 TeV pp, e+e-, muon colliders.



CERN-EP-2019-034.
ATLAS

Highlights of EF03 activities: bb,cc,ss production at lepton colliders

- Electroweak Heavy Flavour (b,c,tau) at the FCC-ee: Patrizia Azzi, Alain Blondel, Mogens Dam, Patrick Janot, Stéphane Monteil, and Guy Wilkinson **LoI**
- Electroweak couplings of heavy and light quarks at future linear e^+e^- colliders: Roman Poeschl, Marcel Vos **LoI**

Presented at this workshop:

- **Top and HF studies at linear colliders:** Roman Poeschl

Highlights of EF03 activities: bb,cc,ss production at lepton colliders

• Top and HF studies at linear colliders Roman Poeschl

Why study lighter quarks?

- Deviations from SM of the order of a few %
 - Effects measurable already at 250 GeV
 - Effects amplified by beam polarisations
 - Effects for tt, bb and cc (and other light fermions)
- One concrete example for importance to measure full pattern of fermion couplings
 - Full pattern only available with beam polarisation

Examples: GUT inspired models Higgs unification model; Randall-Sundrum model modify light quark couplings

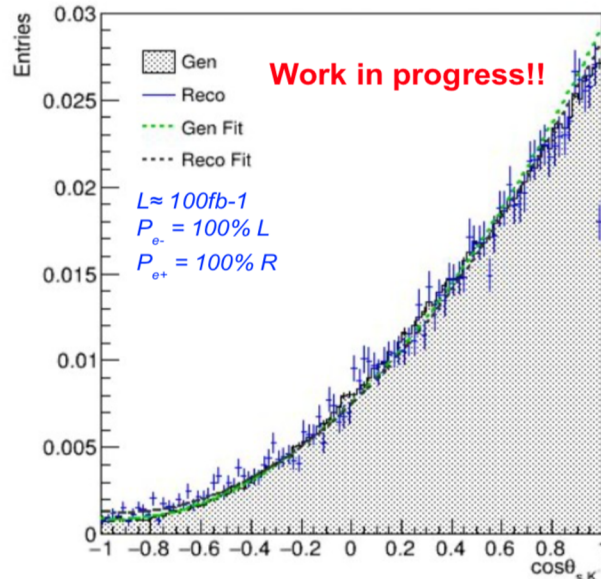


New: ee->ss @ 250 GeV



Y. Okugawa, F. Richard, A. Irlès, R.P.

Full simulation with ILD s/w framework



- This is just an appetiser!
- Analysis is very early stage
 - Full simulation and reconstruction but preselection based on MC truth
 - Analysis will consolidate during Snowmass process!
- Backbone is selection of charged Kaon
 - Strict requirement that charged Kaon with $P_K > 10\text{ GeV}$ is leading particle in jet
- Need to control backgrounds from ee->uu and ee->dd
- Will complete picture on ee->qq
 - The rest is uu/dd that will be indistinguishable and will have to be treated together
- Excellent benchmark for detector
 - "Particle ID is King"

Highlights of EF03 activities: bb,cc,ss production at lepton colliders

- Top and HF studies at linear colliders Roman Poeschl

HQ at ILC/CLIC – Overview on status of analyses



	\sqrt{s} -250 GeV	Threshold	Continuum (≥ 380 GeV)	Comment
ee->tt (electroweak)	N/A	Not covered	Not covered	<ul style="list-style-type: none">• ILC/CLIC Papers exist• CLIC380 close(r) to threshold• ee->tt fully hadronic is not covered (and difficult!)• ee->tt semi-leptonic needs re-assessment of systematic uncertainties
ee->tt (top mass)	N/A	Not covered	Covered	<ul style="list-style-type: none">• Many studies and papers exist• However uncovered aspects (AFB, at threshold, polarisation effects, ...)• Top mass in continuum requires full sim. study
ee->bb	Covered		Covered	<ul style="list-style-type: none">• 250 GeV: paper publication in progress• 500 GeV freshly started
ee->cc	Covered		Covered	<ul style="list-style-type: none">• 250 GeV: paper publication in progress• 500 GeV freshly started
ee->ss	Covered		Not covered	<ul style="list-style-type: none">• 250 GeV: freshly started

The picture is likely to be incomplete! Please let me know if everything is missing

Highlights of EF03 activities: Couplings and EFT fits (with EF04)

- ILC: EFT fit for top and bottom EW couplings: Gauthier Durieux, Martin Perello , Roman Poeschl
- The top quark (EW) couplings at future colliders: Marcel Vos
- Electroweak couplings of heavy and light quarks at future linear e^+e^- colliders: Roman Poeschl, Marcel Vos **Lol**
- Novel constraints on EFT in the top sector: Alexander Grohsjean, James Keaveney, **Lol, paper:** James Keaveney, <https://arxiv.org/abs/2107.01053>

Presented at this workshop:

- **Global fits for top operators:** Eleni Vryonidou
- **EFT studies in the top quark sector (and beyond):** Nuno Castro

Highlights of EF03 activities: Top EFT fits

- EFT studies in the top quark sector (and beyond): Nuno Castro

Effective field theory in the top quark sector

$t\bar{t}$ operators

- Observables: **R**ate, **D**istribution, **A**symmetries, **P**olarization, **S**pin correlation

Linear

$$O_{tG} = (\bar{Q}\sigma^{\mu\nu}T^A t) \tilde{\phi} G_{\mu\nu}^A$$

$$O_{Qq}^{1,8} = (\bar{Q}\gamma_\mu T^A Q)(\bar{q}_i\gamma^\mu T^A q_i)$$

$$O_{Qq}^{3,8} = (\bar{Q}\gamma_\mu T^A \tau^I Q)(\bar{q}_i\gamma^\mu T^A \tau^I q_i)$$

$$O_{tu}^8 = (\bar{t}_L\gamma_\mu T^A t)(\bar{u}_i\gamma^\mu T^A u_i)$$

$$O_{td}^8 = (\bar{t}_L\gamma_\mu T^A t)(\bar{d}_i\gamma^\mu T^A d_i)$$

$$O_{Qu}^8 = (\bar{Q}\gamma_\mu T^A Q)(\bar{u}_i\gamma^\mu T^A u_i)$$

$$O_{Qd}^8 = (\bar{Q}\gamma_\mu T^A Q)(\bar{d}_i\gamma^\mu T^A d_i)$$

$$O_{tq}^8 = (\bar{q}_i\gamma_\mu T^A q_i)(\bar{t}_L\gamma^\mu T^A t)$$

Quadratic

$$O_{Qq}^{1,1} = (\bar{Q}\gamma_\mu Q)(\bar{q}_i\gamma^\mu q_i)$$

$$O_{Qq}^{3,1} = (\bar{Q}\gamma_\mu \tau^I Q)(\bar{q}_i\gamma^\mu \tau^I q_i)$$

$$O_{tu}^1 = (\bar{t}_L\gamma_\mu t)(\bar{u}_i\gamma^\mu u_i)$$

$$O_{td}^1 = (\bar{t}_L\gamma_\mu t)(\bar{d}_i\gamma^\mu d_i)$$

$$O_{Qu}^1 = (\bar{Q}\gamma_\mu Q)(\bar{u}_i\gamma^\mu u_i)$$

$$O_{Qd}^1 = (\bar{Q}\gamma_\mu Q)(\bar{d}_i\gamma^\mu d_i)$$

$$O_{tq}^1 = (\bar{q}_i\gamma_\mu q_i)(\bar{t}_L\gamma^\mu t)$$

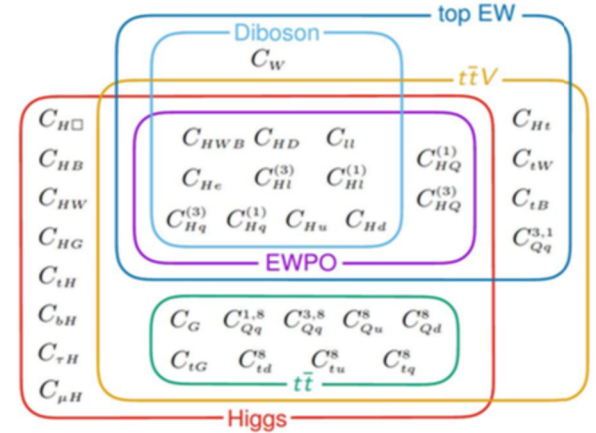
Four-fermion in V/A basis

$$4 C_{VV}^{u,8} = C_{Qq}^{1,8} + C_{Qq}^{3,8} + C_{tu}^8 + C_{tq}^8 + C_{Qu}^8$$

$$4 C_{AA}^{u,8} = C_{Qq}^{1,8} + C_{Qq}^{3,8} + C_{tu}^8 - C_{tq}^8 - C_{Qu}^8$$

$$4 C_{AV}^{u,8} = -(C_{Qq}^{1,8} + C_{Qq}^{3,8}) + C_{tu}^8 + C_{tq}^8 - C_{Qu}^8$$

$$4 C_{VA}^{u,8} = -(C_{Qq}^{1,8} + C_{Qq}^{3,8}) + C_{tu}^8 - C_{tq}^8 + C_{Qu}^8$$

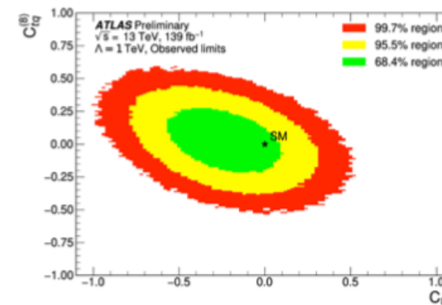


$t\bar{t}$ operators: differential measurements

[slide by Cen Zhang]

Also studied: single top and $\bar{t}tV$ operators

Focus changing to global fits



Wilson coefficient	Marginalised 95% intervals		Individual 95% intervals		
	Expected	Observed	Expected	Observed	Global fit [2105.00006]
C_{tG}	[-0.44, 0.44]	[-0.68, 0.21]	[-0.41, 0.42]	[-0.63, 0.20]	[0.007, 0.111]
$C_{tq}^{(8)}$	[-0.35, 0.35]	[-0.30, 0.36]	[-0.35, 0.36]	[-0.34, 0.27]	[-0.40, 0.61]

Highlights of EF03 activities: Top EFT fits (jointly with EF01, EF04)

- Global fits for top operators: Eleni Vryonidou

Global EFT fits in top physics

Future directions (2)

Future colliders:

- Unlike the Higgs and EW sectors, limited work on HL-LHC, FCC-hh projections for top operators, need for global analyses
- Truly global fits for future colliders as typically only subsets of operators considered
- Combination of top+Higgs for future colliders, including 1-loop effects
- Systematic comparison prospects of different future colliders (ILC, FCC-ee, CEPC and different energies), using a common setup and common set of operators

Highlights of EF03 activities: Couplings and EFT fits (jointly with EF04)

Presented at EF03/EF04 workshop in Jan. 2021: <https://indico.fnal.gov/event/46514/>

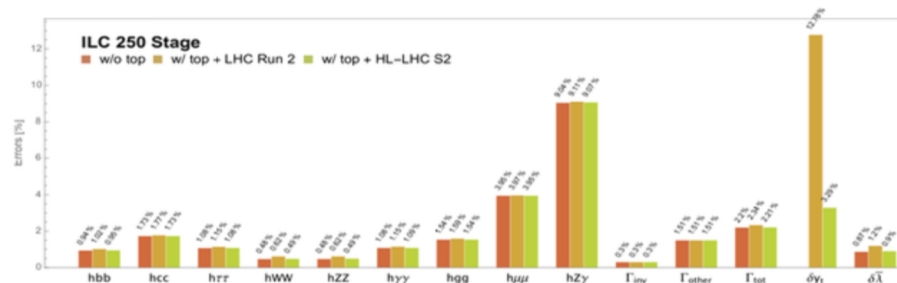
- The top quark (EW) couplings at future colliders: Marcel Vos

Grand, global SM EFT fits

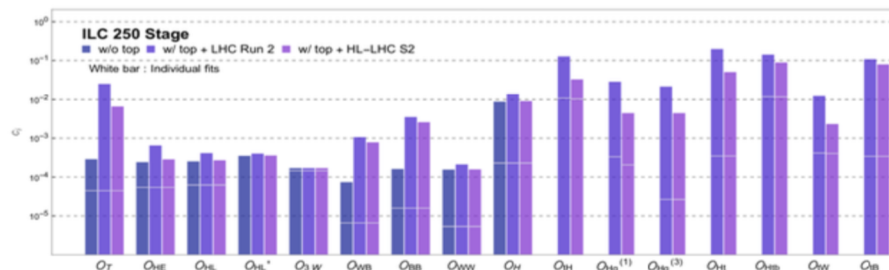
S. Jung, J. Lee, M. Perelló, J. Tian, M.V., arXiv:2006.14631

Top and bottom EW couplings affect 250 GeV Higgs fit considerably

*Physical Higgs couplings
largely shielded from extra
degrees of freedom*



*Limits on Wilson coefficients
are affected by inclusion of
top operators, even with the
most optimistic HL-LHC
prospects*



[See also S. Jung]

Snowmass EF03/04, 29/01/2021

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Highlights of EF03 activities: Top and HF in PDFs (with EF06)

- Constraining heavy flavor PDFs at hadron colliders: Marco Guzzi, Timothy Hobbs, Pavel Nadolsky, Laura Reina, Doreen Wackeroth, Keping Xie, C.-P. Yuan **LoI**

Presented at this workshop:

- **The role of top quark observables in PDFs:** CT: Marco Guzzi; MSHT: Robert Thorne; NNPDF: Emanuele Nocera
- **Simultaneous extraction of alphas and m_{top} from tt differential distributions:** Matthew Lim
- **Experimental and phenomenological issues relevant for PDF extractions from top differential distributions** Amanda Cooper Sarkar

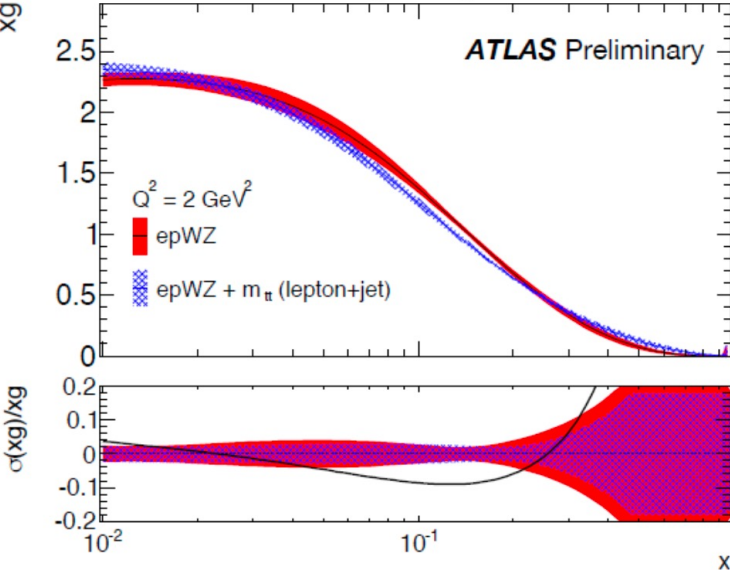
Highlights of EF03 activities: Top in PDFs (jointly with EF06)

PDF fitting t-tbar data- experimental considerations: Amanda Cooper Sarkar

The importance of the correlation of systematic uncertainties:

- between data points within a spectrum
- between different spectra from a single analysis
- between different spectra from different analyses, different processes

The most constraining top distributions are p_T^t , y_t , $y_{t\bar{t}}$, $m_{t\bar{t}}$ and they mostly constrain the high-x gluon



$$\chi^2 = \sum_{ik} \left(D_i - T_i \left(1 - \sum_j \gamma_{ij} b_j \right) \right) C_{\text{stat}, ik}^{-1} (D_i, D_k) \left(D_k - T_k \left(1 - \sum_j \gamma_{kj} b_j \right) \right) + \sum_j b_j^2$$

The treatment of correlated systematics as nuisance parameters means that they can introduce correlated shifts in the predictions. Examining the shifts due to these 3 sources shows that the $m_{t\bar{t}}$ spectrum induces an opposite shift to the other three spectra, when the spectra are fitted separately. When fitting together the shifts are forced to be the same --if 100% correlation is assumed between the spectra. E.g. the common nuisance parameter for the Parton Shower uncertainty when fitting p_T^t and $m_{t\bar{t}}$ together is -0.32 ± 0.10 , which suits neither spectrum.

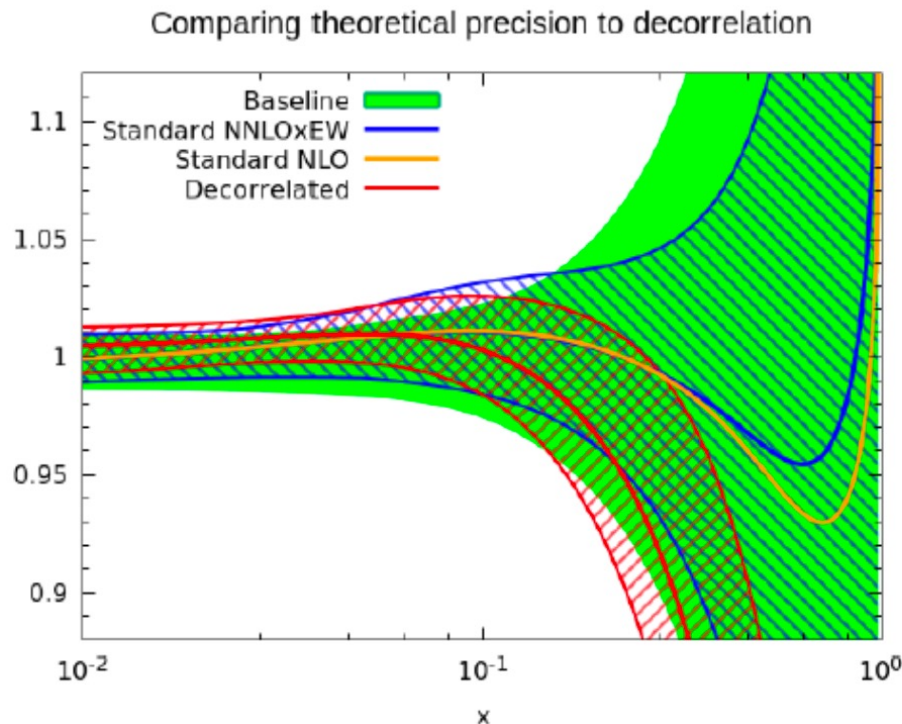
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The effect of decorrelation is dramatic for the p_T^t and $m_{t\bar{t}}$ spectra, now that the shifts are allowed to be different. (The separate nuisance parameters are -0.47 for p_T and +0.10 for m_{tt}). The resultant χ^2 is close to the sum of the χ^2 of the separate fits (11.3)

Highlights of EF03 activities: Top and HF in PDFs (jointly with EF06)

- PDF fitting t - \bar{t} data- experimental considerations : Amanda Cooper Sarkar

But for the arxiv:1909.10541 study decorrelating parton shower between all 4 spectra and using decorrelation within the rapidity spectra we see that the effect can be larger than the NLO to NNLO difference.



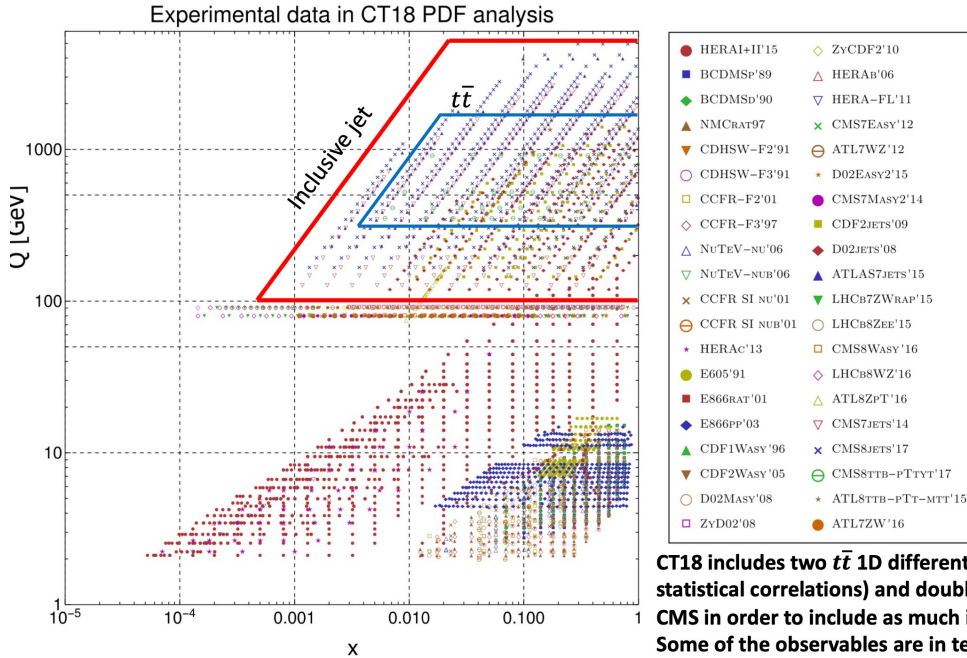
- Most useful to present information on correlated uncertainties
- Naming convention for source of systematic uncertainties.
- How about inter-data-set correlations: not yet taking into account in PDF fits

If we want 1% accuracy on PDFs this matters!

Highlights of EF03 activities: Top in PDFs (jointly with EF06)

- The role of top quark observables in PDFs: CT: Marco Guzzi

$t\bar{t}$ production kinematics in CT18

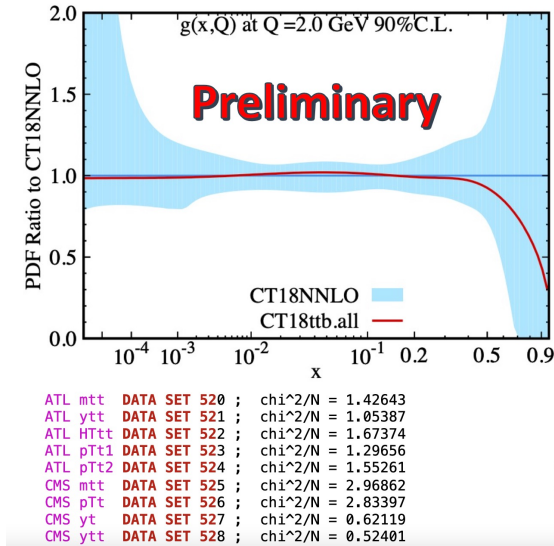


Jet and $t\bar{t}$ complement each other in the kinematic plane. They impact the **gluon PDF at large x**. Important to disentangle the effect due to jet production and top-quark data.

Top and jet Data in CT18

Top-quark
 1511.04716 ATLAS 8 TeV $t\bar{t}$ pt diff. distributions
 1511.04716 ATLAS 8 TeV $t\bar{t}$ mt diff. distributions
 1703.01630 CMS 8 TeV $t\bar{t}$ (pT, yt) 2d diff. distrib.
 Jet production
 1406.0324 CMS incl. jet at 7 TeV with R=0.7
 1410.8857 ATLAS incl. jet at 7 TeV with R=0.6
 1609.05331 CMS incl. jet at 8 TeV with R=0.7

Global fit: Impact from 13 TeV ATLAS+CMS $t\bar{t}$ data:



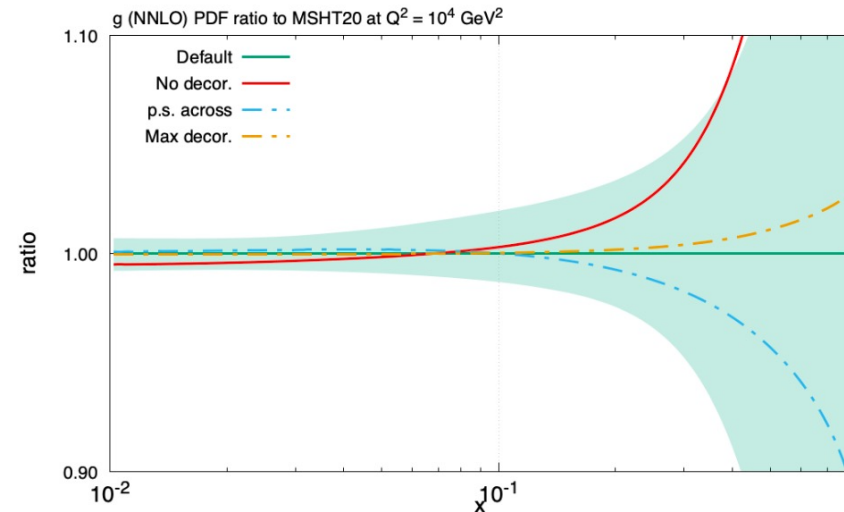
- Detailed information on both **covariance and nuisance parameter** representations for experimental errors is critical for full exploitation of data in PDF determinations
- Critical to Constrain m_t , α_s , g correlations

Highlights of EF03 activities: Top in PDFs (jointly with EF06)

- The role of top quark observables in PDFs: MSHT2020: Robert Thorne

Include all our recent LHC data updates in the fit at NNLO (for default $\alpha_S(M_Z^2) = 0.118$).

	no. points	NNLO χ^2/N_{pts}
D0 W asymmetry	14	0.86
$\sigma_{t\bar{t}}$ Tevatron +CMS+ATLAS 7, 8TeV	17	0.85
LHCb 7+8 TeV $W + Z$	67	1.48
LHCb 8 TeV e	17	1.54
CMS 8 TeV W	22	0.58
ATLAS 7 TeV jets $R = 0.6$	140	1.59
CMS 7 TeV $W + c$	10	0.86
ATLAS 7 TeV W, Z	61	1.91
CMS 7 TeV jets $R = 0.7$	158	1.11
ATLAS 8 TeV $Z p_T$	104	1.81
CMS 8 TeV jets	174	1.50
ATLAS 8 TeV $t\bar{t} \rightarrow l + j$ single-diff	25	1.02
ATLAS 8 TeV $t\bar{t} \rightarrow l^+ l^-$ single-diff	5	0.68
ATLAS 8 TeV high-mass Drell-Yan	48	1.18
ATLAS 8 TeV $W^{+,-} + \text{jet}$	32	0.60
CMS 8 TeV $(d\sigma_{t\bar{t}}/dp_{T,t} dy_t)/\sigma_{t\bar{t}}$	15	1.50
ATLAS 8 TeV W^{+}, W^{-}	22	2.61
CMS 2.76 TeV jets	81	1.27
CMS 8 TeV $t\bar{t} y_t$ distribution	9	1.47
ATLAS 8 TeV double differential Z	59	1.45
Total, LHC data	1328	1.33
Total, all data	4363	1.17



Effects on PDFs of different treatments of systematic uncertainties: no decorrelation, parton shower across, max. decorrelation

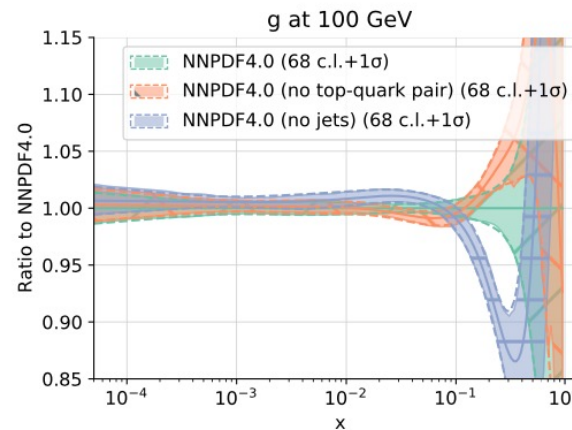
Fit quality generally good. Relatively poor χ^2 values for some sets seemingly observed by other groups, rectified by treatment of correlated uncertainties.

Highlights of EF03 activities: Top in PDFs (jointly with EF06)

- The role of top quark observables in PDFs: NNPDF: Emanuele Nocera

NNPDF4.0: more LHC data

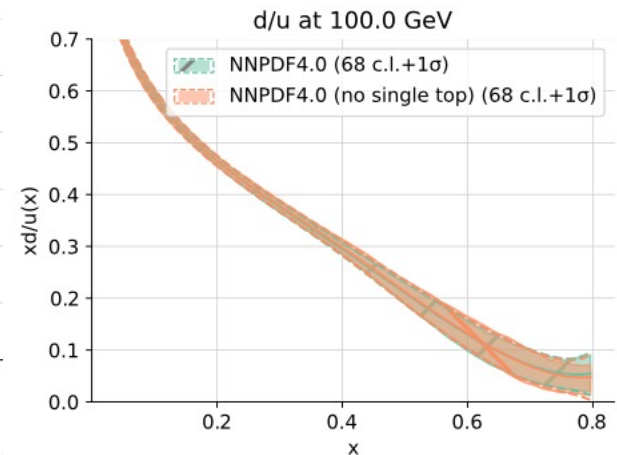
Dataset	N_{dat}	$\chi^2_{4.0}$
CMS $\sigma_{t\bar{t}}^{\text{tot}}$ 5 TeV	1	0.54
ATLAS $\sigma_{t\bar{t}}^{\text{tot}}$ 7 TeV	1	1.59
CMS $\sigma_{t\bar{t}}^{\text{tot}}$ 7 TeV	1	1.06
ATLAS $\sigma_{t\bar{t}}^{\text{tot}}$ 8 TeV	1	0.02
CMS $\sigma_{t\bar{t}}^{\text{tot}}$ 8 TeV	1	0.26
ATLAS $\sigma_{t\bar{t}}^{\text{tot}}$ 13 TeV (139 fb^{-1})	1	0.51
CMS $\sigma_{t\bar{t}}^{\text{tot}}$ 13 TeV	1	0.06
ATLAS $\ell+j$ 8 TeV ($1/\sigma d\sigma/dy_t$)	4	3.22
ATLAS $\ell+j$ 8 TeV ($1/\sigma d\sigma/dy_{t\bar{t}}$)	4	3.77
ATLAS 2ℓ 8 TeV ($1/\sigma d\sigma/dy_{t\bar{t}}$)	5	1.61
CMS $\ell+j$ 8 TeV ($1/\sigma d\sigma/dy_{t\bar{t}}$)	9	1.23
CMS 2ℓ 8 TeV ($1/\sigma d\sigma/dy_{t\bar{t}} dm_{t\bar{t}}$)	16	1.03
CMS $\ell+j$ 13 TeV ($d\sigma/dy_t$)	11	0.63
CMS $t\bar{t} 2\ell$ 13 TeV ($d\sigma/dy_t$)	10	0.52
ATLAS dijets 7 TeV, $R = 0.6$	90	2.15
CMS dijets 7 TeV	54	1.81
ATLAS incl. jets 8 TeV, $R = 0.6$	171	0.69
CMS incl. jets 8 TeV	185	1.19
Total	4618	1.16



Dataset significantly extended in NNPDF4.0
(top and jets)

top: 40 data points more than NNPDF3.1
jet: 336 data points more than NNPDF3.1

Competing pulls of top and jets



Single top production not yet
precise enough to constrain
PDF

Highlights of EF03 activities: Top and HF in PDFs (with EF06)

- Simultaneous extraction of α_s and m_{top} from tt differential distributions:
Matthew Lim

- ▶ 8 TeV data from ATLAS and CMS collected in Run 1
- ▶ Differential distributions of tops reconstructed from lepton+jets analyses, common binning
- ▶ Transverse momentum p_t^T , invariant mass $M_{t\bar{t}}$, single and pair rapidities $y_t, y_{t\bar{t}}$
- ▶ Absolute and normalised distributions—separate data sets from ATLAS, only normalised from CMS (absolute inferred)
- ▶ Theory values of $\sigma_{t\bar{t}}$ calculated using top++2.0 at NNLO with NNLL resummation of soft gluons
- ▶ ‘Best’ value from combining two ATLAS distributions and averaging CT14 results.
- ▶ $\alpha_s = 0.1159^{+0.0013}_{-0.0014}$, $m_t = 173.8^{+0.8}_{-0.8} \text{ GeV}$.
- ▶ Prospects for future inclusion of theory uncertainties due to MHO.
- ▶ Find noticeable differences between
 - ▶ ATLAS and CMS
 - ▶ Different PDF choices
 - ▶ Different distributionsindicating large sensitivity to all factors—data, PDF and kinematics.
- ▶ In order to reconcile differences/arrive at best values,
 - ▶ Restrict $0.115 \leq \alpha_s \leq 0.120$ and $170.0 \leq m_t \leq 175.0 \text{ GeV}$ ($\pm \sim 3\sigma$ around world average);
 - ▶ Perform a weighted average over various extractions.
- ▶ Most pragmatic way to include effects due to MHO is *all* NNPDF.
 - ▶ Assume Gaussian uncertainties, construct a theory covariance matrix.
- ▶ More sophisticated approach (see Tackmann, Les Houches 2019):
 - ▶ Regard missing higher order terms as nuisance parameters.
 - ▶ $\sigma = c_0 + \alpha_s(\mu)[c_1 + \alpha_s(\mu)c_2 + \dots]$
 - ▶ In the simplest case c_2 is a number, more generally a function.
 - ▶ Correct correlations obtained, when multiple parameters involved CLT implies total theory uncertainty is Gaussian.

Highlights of EF03 activities: SM predictions

- EW higher order calculations for top quark and heavy flavor production at lepton colliders: Emi Kou
- A detailed comparison of QCD modelling in $pp \rightarrow ttW$ production: G. Bevilacqua, H. Bi, F. Febres-Cordero, H.B. Hartanto, M. Kraus, J. Nasufi, L. Reina, M. Worek **Lol**

Presented at this workshop:

- **Soft gluons in top processes (tt and tW) at high energies:** Nikolaos Kidonakis

Highlights of EF03 activities: SM predictions

- Soft gluons in top processes (tt and tW) at high energies: Nikolaos Kidonakis

Soft-gluon corrections

partonic processes (in general $2 \rightarrow n$)

$$f_1(p_1) + f_2(p_2) \rightarrow t(p_t) + X$$

define $s = (p_1 + p_2)^2$, $t = (p_1 - p_t)^2$, $u = (p_2 - p_t)^2$ and $s_4 = s + t + u - p_t^2$

At partonic threshold $s_4 \rightarrow 0$

Soft corrections $\left[\frac{\ln^k(s_4/m_t^2)}{s_4} \right]_+$ with $k \leq 2n - 1$ for the order α_s^n corrections

Resum these soft corrections \rightarrow finite-order expansions-no prescription

Approximate NNLO (aNNLO) and N³LO (aN³LO) predictions

for cross sections and differential distributions (single and double) soft-gluon corrections dominant at LHC for total & differential cross sections

$t\bar{t}$ at high energies - preliminary results ($\mu = m_t$, same pdf)

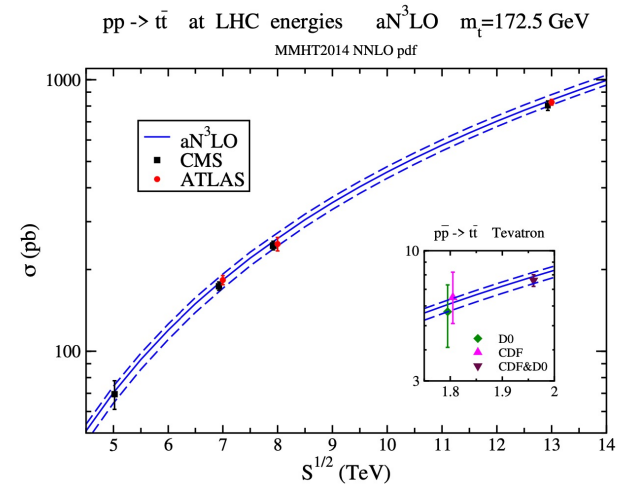
	14 TeV	20 TeV	30 TeV	40 TeV	50 TeV	100 TeV
NLO/LO	1.50	1.51	1.52	1.53	1.54	1.58
aNLO/NLO	0.99	0.98	0.97	0.96	0.95	0.92
NNLO/NLO	1.11	1.11	1.11	1.11	1.11	1.10
aNNLO/NNLO	1.00	1.00	0.99	0.99	0.99	0.98
aN ³ LO/NNLO	1.03					

where

aNLO = LO + soft-gluon NLO corrections

aNNLO = NNLO + soft-gluon NNLO corrections

aN³LO = NNLO + soft-gluon N³LO corrections



Highlights of EF03 activities: Top physics at a muon collider

Presented at this workshop:

- Top quark physics at a muon collider: Tobias Thiel
- Precision studies at a muon collider: Patrick Meade (jointly with EF01/EF04)

Highlights of EF03 activities: Top physics at a muon collider

- **Precision studies at a muon collider:** Patrick Meade (jointly with EF01/EF04)
- Vector boson fusion at multi-TeV muon collider: Antonio Costantini, Federico De Lillo, Fabio Maltoni, Luca Mantani, Olivier Mattelaer, Richard Ruiz and Xiaoran Zhao, arxiv:2005:10289

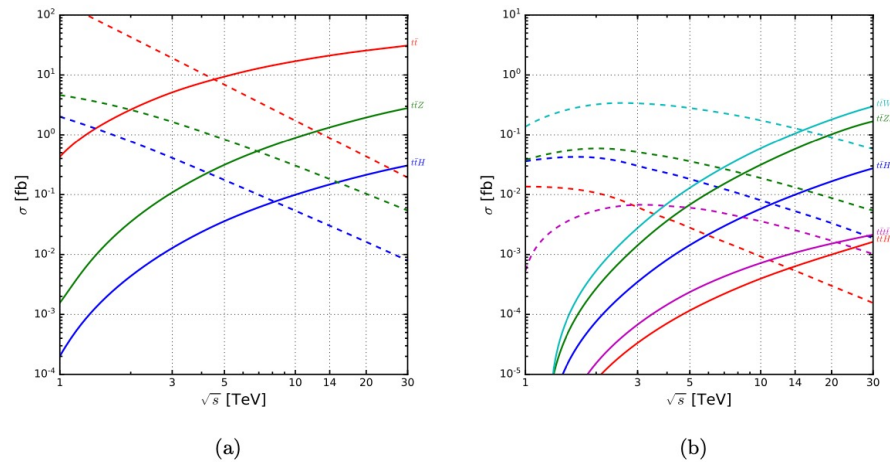


Figure 3. W^+W^- fusion (solid) and analogous s -channel annihilation (dashed) cross sections σ [fb] for (a) $t\bar{t}X$ and (b) $t\bar{t}XX$ associated production as a function of collider energy \sqrt{s} [TeV].

s -channel annihilation rates categorically scale and decrease with collider energy at least as $\sigma \sim 1/s$, when collider energies are far beyond kinematic threshold. This is contrary to VBF processes where cross sections mildly increase with collider energy at least as a power of $\log(s/M_{W2})$, in the high energy limit.

Other EF03 activities

- Prospects for the 4top Process: Stephen Wimpenny
- $t\bar{t}W$ production: a very complex process: Marcos Miralles Lopez, Maria Moreno Llacer
- Precise predictions for top-quark flavor-changing neutral interactions at future lepton colliders: Gauthier Durieux, Stefano Frixione, Benjamin Fuks, Hua-Sheng Shao, Liaoshan Shi, Marco Zaro, Cen Zhang, and Xiaoran Zhao **Lol**
- Probing top quark FCNC couplings $tq\gamma$, tqZ at future e^+e^- collider: Peiwen Wu **Lol**
- Top quark physics at FCC-ee: J. Andrea, P. Azzi, B. Fuks **Lol**
- Top-Quark and Electroweak Physics at LHeC and FCC-eh: N. Armesto, O. Behnke, D. Britzger, O. Cakir, M. Klein, C. Schwanenberger, H. Spiessberger **Lol**
- Study on the discovery potential of all-hadronic searches for $t\bar{t}$ resonances at future colliders: Johan Bonilla, Robin Erbacher, Christine Mclean, Meg Morris, Salvatore Rappoccio, A.C. Malik Williams **Lol**

Final remarks

- Many opportunities to contribute to Top/HF production physics
 - So far most input from ILC and HL-LHC,
 - Top physics potential talks from FCC-ee, LHeC and FCC-eh
 - Study top at other colliders (new: muon collider)
 - Need many more HL-LHC studies to explore full program
 - Across topical group boundaries
- We invite you to contribute to top/HF production studies
 - EF03 wiki page at https://snowmass21.org/energy/heavy_flavour
 - Email the conveners: schwier@msu.edu, dw24@buffalo.edu
 - Mailing list SNOWMASS-EF-03-TOP_HEAVY-FLAVOR@FNAL.GOV
 - Looking for presentations at our biweekly meetings
- Informal (incomplete) list of projects, possible collaborations, open questions, etc. <https://docs.google.com/document/d/17aPp9XpJAlmmPlnPNtgV21rG2zEiFS2IHkO-ooC4rcQ>
- See EF03 wiki page for full list of Letters of Interest